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**Exercise 1.**

(7=2+3+2 points)

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Consider the following Simple-TSP task. The set of facts is  $P = \{at(l_1), at(l_2), at(l_3), at(l_4), at(l_5), visited(l_1), visited(l_2), visited(l_3), visited(l_4), visited(l_5)\}$ . The initial state is  $I = \{at(l_1)\}$ . The goal is  $G = \{visited(l_1), visited(l_2), visited(l_3), visited(l_4), visited(l_5)\}$ . The set of actions is  $A = \{visit(x, y) \mid 1 \leq x \neq y \leq 5\}$  where  $visit(x, y) = (\{at(x)\}, \{at(y), visited(y)\}, \{at(x)\})$ .

1. Are there dead ends? Prove your answer, using as much as possible the lemmas in “Local Search Topology”, slides 53–63.
2. Are there local minima under  $h^+$ ? Prove your answer, using as much as possible the lemmas in “Local Search Topology”, slides 53–63.
3. What is the maximal exit distance under  $h^+$ ? Prove your answer, not necessarily using the terminology on the slides.

Note: Both 1. and 2. *can* be proved using lemmas from the lecture. If you do not use those lemmas, then points will be subtracted.

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**Exercise 2.**

(3 points)

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Prove hardness in the theorem on “Local Search Topology” slide 52, i.e., prove PSPACE-hardness of DEAD-END. Tip: There is a very simple proof that goes via a reduction from PLANSAT (“Planning Formalisms”, slide 27); given an arbitrary STRIPS task  $(P, A, I, G)$ , you can modify that task to  $(P', A', I', G')$  in a way so that  $(P', A', I', G')$  contains a dead end iff  $(P, A, I, G)$  is unsolvable.