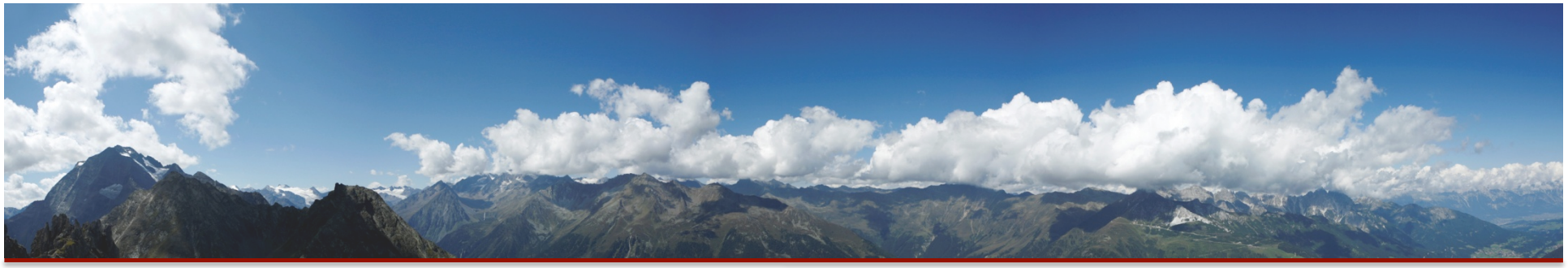
Intelligent Systems

Problem Solving Methods



Where are we?

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1	Introduction
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3	Predicate Logic
4	Theorem Proving, Description Logics and Logic Programming
5	Search Methods
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Agenda

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- Technical Solution
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MOTIVATION

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- In order to allow automation in the achievement of complex problems we should like a general solution with the following characteristics:

Knowledge

– Based on *reasoning* with *knowledge;*

– Works with a *declarative*, rather than an algorithmic, representation of knowedge;

Process

– Represents knowledge on the problem-solving *process*, i.e., the dynamics of the solution;

Reuse

– Allows *reuse* of reasoning knowledge;

– Abstracts from implementation and *domain* to increase reusability.

- As a motivating example we consider the task (i.e., goal) of *parametric design*, which can be defined over:
  - **Design space** – the space that contains all possible designs;
  - **Requirements** – a finite set of which are assumed to be provided by the user;
  - **Constraints** – a finite set of which model additional conditions for a valid design;
  - **Preference** – a function over the design space which can be used to discriminate between different solutions.

Motivating Example

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- *Domain knowledge* is implicit in the parametric design description in several places:
  - **Design space** – the concrete definition of the design space is domain specific knowledge
  - Requirements
  - **Constraints** – domain knowledge concerning regularities in the domain in which the design is constructed;
  - Preference

- Formally, a design artifact is described by a set of attribute-value pairs.

  Let $A_1, ..., A_n$ be a fixed set of parameters with fixed ranges $R_1, ..., R_n$:

  - **Design space** is the cartesian product $R_1 \times ... \times R_n$;
  - **Requirements** – a relation R which defines a subset of this space;
  - **Constraints** – a relation C which defines a subset of this space;
  - **Preference** – a partial function P having all possible designs as its domain and preference values as its range.

Motivating Example

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design space

Visually we represent these aspects as the *domain view*

constraints

requirements

preference

domain view (i.e., static knowledge role)

- Several types of design are implicitly defined by these aspects of the problem:
  - **Possible design** – An element in design space ($\in R_1 \times ... \times R_n$);
  - **Desired design** – A design that fulfills all requirements ($\in R$);
  - **Valid design** – A design that fulfills all constraints ($\in C$);
  - **Solution** – A design which is *desired* and *valid* ($\in R \cap C$);
  - **Optimal solution** - A solution for which no other solution which has a higher preference value exists
    (any solution x such that $\forall y \in R_1 \times ... \times R_n . P(y) \leq P(x)$).

There is also the possible extension:

- **Acceptable solution** - Given a threshold t, an acceptable solution is any solution x such that $P(x) > t$.

Motivating Example

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design space

Visually we represent these as *dynamic* data in a store:

possible design

constraints

requirements

valid design

desired design

solution

data store (i.e., dynamic knowledge role)

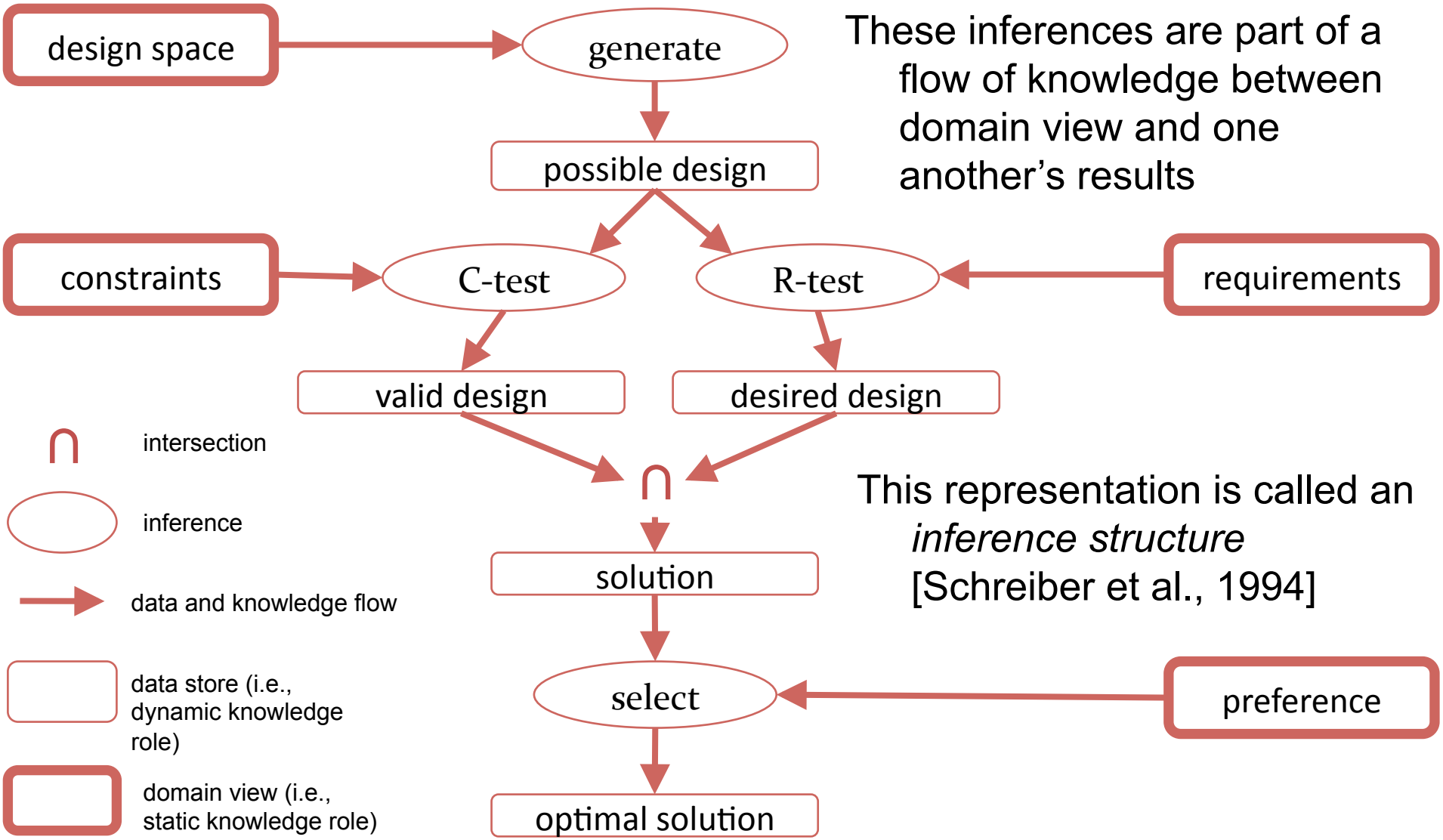
preference

domain view (i.e., static knowledge role)

optimal solution

- An inefficient naive approach to parametric design is called *generate & test*, which depends on the following inferences:
  - **generate** – requires knowledge that describes what constitutes a possible design (i.e., the design space);
  - **R-test** – requires knowledge that describes which possible designs are desired (i.e. the user requirements);
  - **C-test** – requires knowledge that describes which possible designs are valid (i.e., the domain constraints);
  - **select** – requires knowledge that evaluates solutions (i.e., knowledge that describes what constitutes a preferred design).

Motivating Example



These inferences are part of a flow of knowledge between domain view and one another's results

This representation is called an *inference structure* [Schreiber et al., 1994]

- This naive solution can also be represented as:

  possible design := **generate**$_{all}$;
  valid design := **C-test**(possible design);
  desired design := **R-test**(possible design);
  solution := valid design ∩ desired design;
  optimal solution := **select**(solution)

- Using the definition of acceptable solution this can be made somewhat more efficient as:

  repeat
    possible design := **generate**$_{one}$;
    valid design := **C-test**(possible design);
    desired design := **R-test**(possible design);
    solution := valid design ∩ desired design;
    acceptable solution := **select**(solution)
  until Ø ≠ acceptable solution

Lessons from Example

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- generate & test has the following characteristics:
  - it separates the different types of knowledge;
  - it is not efficient (all possible designs are generated);
  - It may not terminate if the design space is infinite.
- From the literature on expert systems [Stefik et al., 1983]:
  - “an important issue is the distribution of knowledge between the generator and the tester: putting as much knowledge as possible into the generator often leads to a more efficient search.”
- A much more clever strategy is therefore to use these knowledge types to guide the generation of possible designs.
- However to do so requires strong assumptions about the domain knowledge.

TECHNICAL SOLUTIONS

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- What are *problem-solving methods (PSMs)*?
  - "Reasoning strategies that gain efficiency through *assumptions.*"

    [Fensel, 2000]
- How can problem-solving methods be described?
  - "[With] operational specifications supplemented [by a formal description of] *competence* and *assumptions*";
  - "using adapters to relate them to the task and domain";
  - "[taking] into account the constraints on the reasoning process and the complexity of the task".
- How can problem-solving methods be reused?
  - Using a combination of:
    - "*Inverse verification* to support the explication of context"
    - "and *adapters* to support the adaptation to a new context"

Technical Solution Overview

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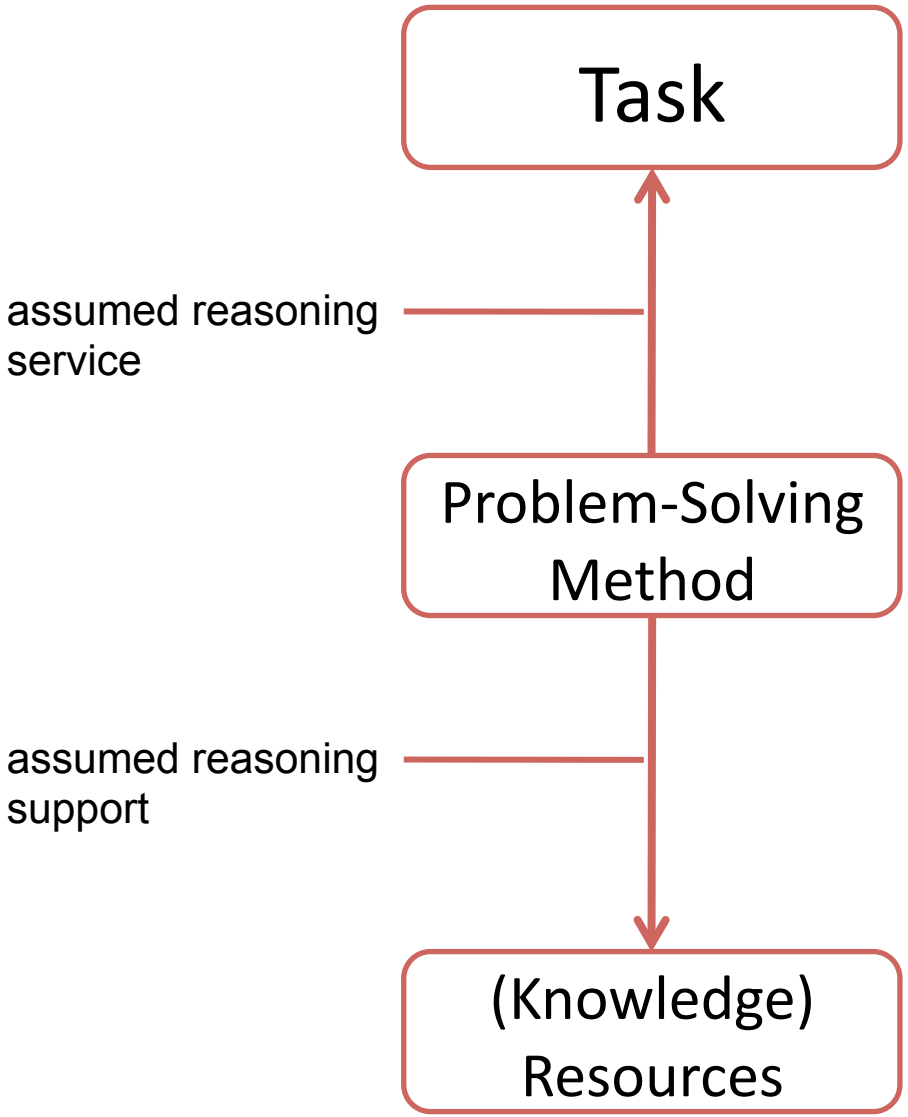
- Assumptions play two roles:
  - they formulate requirements on reasoning support that is assumed by PSMs;
  - they put restrictions on the reasoning support that is provided by PSMs.
- In consequence, assumptions link PSMs with the domain knowledge they use and tasks they are applied to.



Example Revisited

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- We consider again the task of parametric design.
- A more efficient method is named *propose & revise* and depends on the following inferences:
  - **propose** – derives an initial design based on the requirements;
  - **C-test** – as before;
  - **revise** – tries to improve an incorrect design based on the feedback of the C-test step.
- In other words, instead of proposing a complete design which is then repaired, we can also incrementally develop a design and repair it at each step where a constraint violation occurs.

Example Revisited

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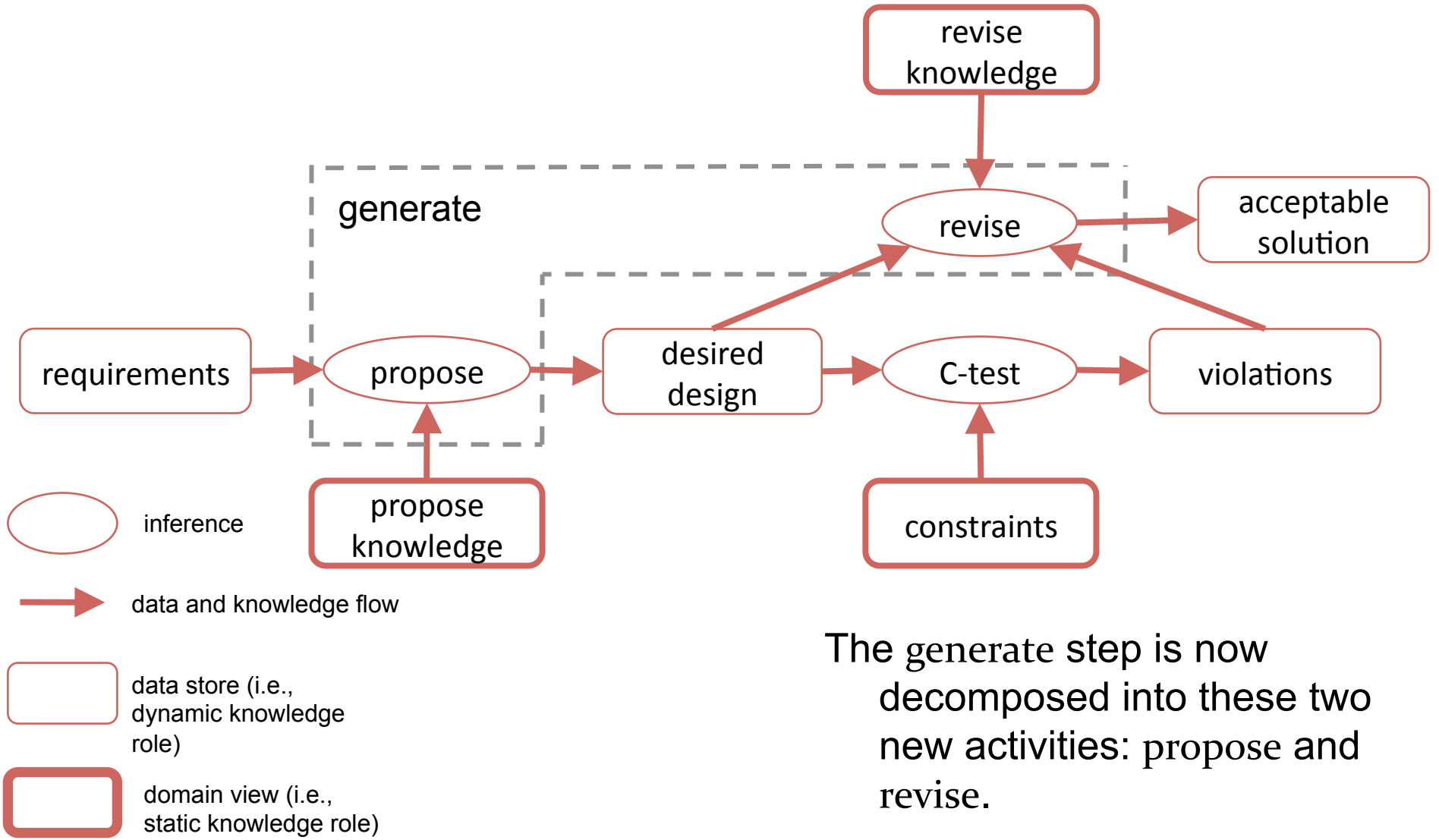

The generate step is now decomposed into these two new activities: propose and revise.

Example Revisited

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- A parameter which should receive a value in the next **propose** step is *nondeterministically* selected:
  - The selection process does not make further assumptions about knowledge that could guide this second selection step
  - The implicit assumption is that this selection does not a affect the performance of the problem solving process and the quality of its result
  - **These are very strong assumptions because to improve performance, heuristic methods are definitely needed**
  - At any time there is either precisely one applicable propose rule or one user input to derive the value of the selected parameter
  - A parameter should not depend on itself (no recursive derivation rules)

Example Revisited

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- **revise** is decomposed into:
  - **select-violation** - nondeterministically selects a constraint violation from those detected by C-test; implicit assumption is that this selection does not influence the performance of the problem solving method and the quality of the result; **strong assumption again**
  - **derive-fixes** - computes the set of all possible fix combinations that could possibly resolve the selected constraint violation; each combination must be finite
  - **select-fix** - selects a fix combination, guided by a cost-function
  - **apply-fix** - applies a fix combination

Example Revisited

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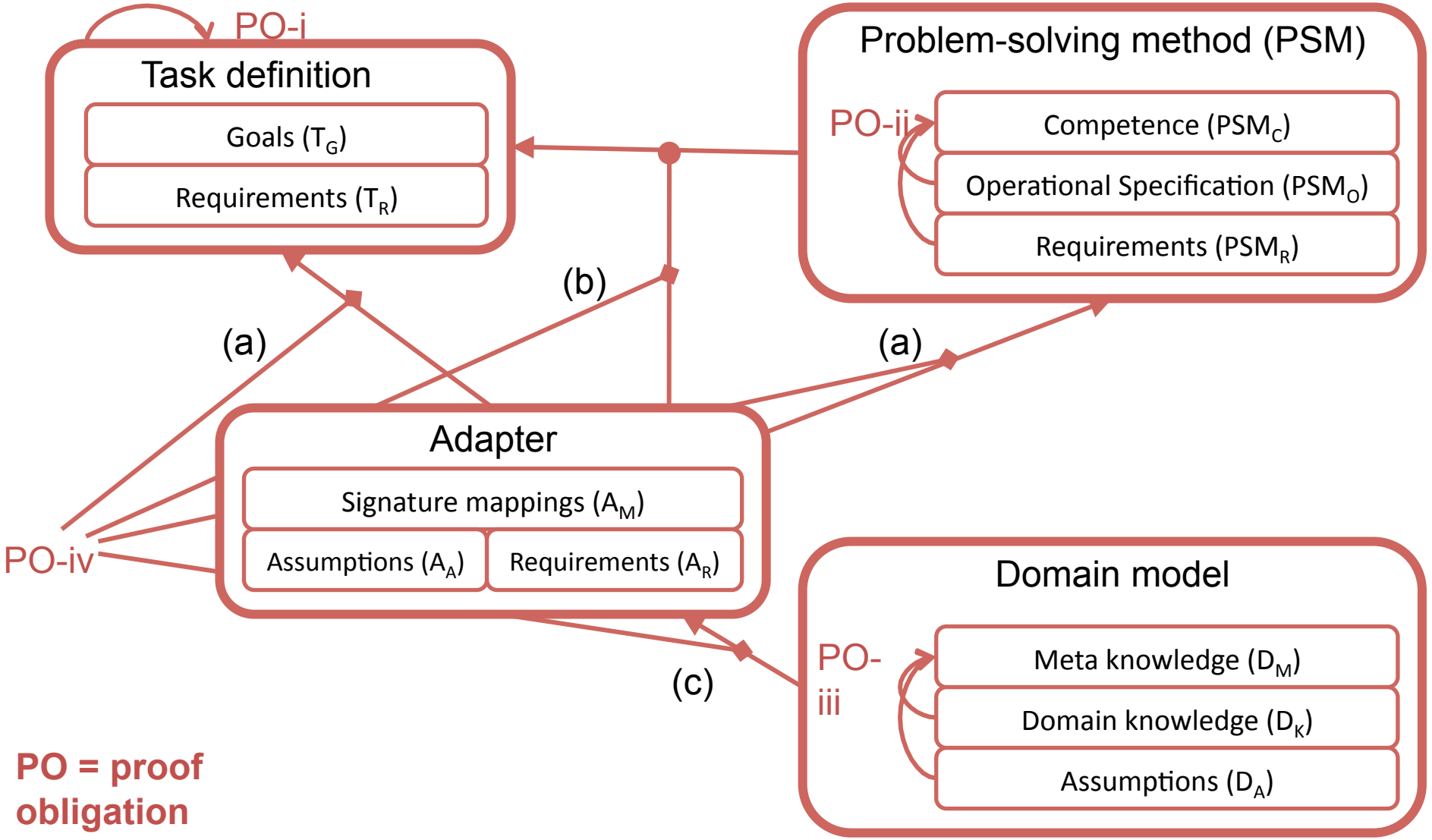
- **Test** – propose & revise does not require an explicit R-test, the method assumes that:
  - propose derives only desired designs;
  - revise delivers designs that are desired or that requirement violations that it does not x must be accepted.
- **Selection** – does not contain such a process concerning user preferences:
  - It assumes that the propose step and the revise step deliver acceptable (or optimal) solutions or that the functionality of the task is reduced to finding an arbitrary solution.

- The main elements of a specification in the PSM framework are:
  - **the task** – specifies the *goals* that should be solved in order to solve a given problem. A second part of a task specification is the definition of *requirements* on domain knowledge;
  - **the problem-solving method** – describes an reasoning steps to perform a task as an *operational specification* separately from a description of the *competence,* and a description of the *requirements* on domain knowledge;
  - **the domain model** – usually ontology-based description in three parts, a meta-level characterisation of properties, the domain knowledge, and (external) assumptions of the domain model;
  - **the adapter** – maps the different terminologies of the task definition, problem-solving method and domain model. Moreover, gives further requirements and assumptions needed to relate the competence of the PSM with the functionality of the task.

Description of Problem-Solving Methods



- Several proof obligations follow the conceptual model of such a specification of a knowledge-based system:
  - **PO-i**: the consistency of the task definition to ensure that a model exists, otherwise one could define an unsolvable problem;
  - **PO-ii**: that the operational specification of the PSM describes a terminating process which has the competence as specified;
  - **PO-iii**: the internal consistency of the domain knowledge and domain model, also that the assumptions on domain knowledge implies its meta-level characterisation;
  - **PO-iv**: relationships between the specification elements –
    a) the requirements of the adapter imply the knowledge requirements of the PSM and task,
    b) the adapter's additional requirements on domain knowledge and assumption guarantee that the competence of the PSM is strong enough for task,
    c) The requirements of the adapter are implied by the meta knowledge of the domain model.

PSM Framework Example

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- To illustrate the description of PSMs we consider search
- Local search can be refined into other versions using adapters, specifically:
  - **Hill-climbing**: a local search algorithm which stops when it has found a *local optimum*, based on recursively considering the *successors* to a start object, selecting better at each stage;
  - **Set-Minimizer**: finds a *minimal* but still *correct subset* of a given set, with respect to hill-climbing –
    - generic 'object' becomes a set,
    - 'successor' relationship is hard-wired,
    - preference is implicit;
  - **Abductive Diagnosis**: receives a set of *observations* as input and delivers a *complete* (explains all input data) and *parsimonious* (no subset of hypotheses explains all observations) *explanation*.

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- Local search can be represented in the following operational specification:

operational specification local search
output := local search(input);
local search(X)
begin
currents := $select_1(X)$;
output := recursion(currents);
end
recursion(X)
begin
successors := generate(X);
new := $select_2(X, successors)$;
if X = new
then output := $select_3(X)$;
else recursion(new);
end

$select_1(x) \subseteq x$

$x \in generate(y) \leftrightarrow x \in input \wedge \exists z.(z \in y \wedge successor(z, x))$

$select_2(y, y') \subseteq y \cup y'$

$\neg \exists x, z . (z \in (y \cup y') \setminus select_2(y, y') \wedge x < z)$

$y \cup y' \neq \varnothing \rightarrow \exists x.(x \in select_2(y, y'))$

$select_3(y) \subseteq y$

$\neg \exists x, z . (z \in (y \setminus select_3(y)) \wedge x \in select_3(y) \wedge x < z)$

$y \neq \varnothing \rightarrow \exists x.(x \in select_3(y))$

endoperational spec

PSM Framework Example

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- Adapters between refinement levels can be represented as follows:

PSM refinement adapter set-minimizer -> abduction-method
correct(x) = complete(x);
input = {h | h is hypothesis};
$H \subseteq H' \rightarrow explain(H) \subseteq explain(H')$
endPSM refinement adapter
PSM refinement adapter hill-climbing -> set-minimizer
correct(input);
$select_1(x) = \{x\}$;
$successor(x, y) \leftrightarrow \exists z . (z \in x \wedge y = x \setminus \{z\})$;
$x < y \leftrightarrow correct(y) \wedge y \subset x$
endPSM refinement adapter
PSM refinement adapter local-search -> hill-climbing
$|select_1(x)| = 1$;
$\neg\exists z . (z \in y' \wedge y < z) \rightarrow select_2(\{y\}, y') = \{y\}$;
$|select_2(\{y\}, y')| = 1$
endPSM refinement adapter

ILLUSTRATION BY A LARGER EXAMPLE

- The Sisyphus-I office allocation problem was the first of a series of test applications for approaches to building knowledge-based systems.
- The aim is to automate the problem-solving behaviour of ‘Siggi’, a hypothetical domain expert .
- Specifically Siggi is required to make assignments of the staff of a research group ‘YQT’ to offices.
- The 4-page problem statement describes the office layout and relevant data about the 15 group members.
- A ‘protocol’ is provided, describing the steps Siggi takes.

Sisyphus-I Office Layout

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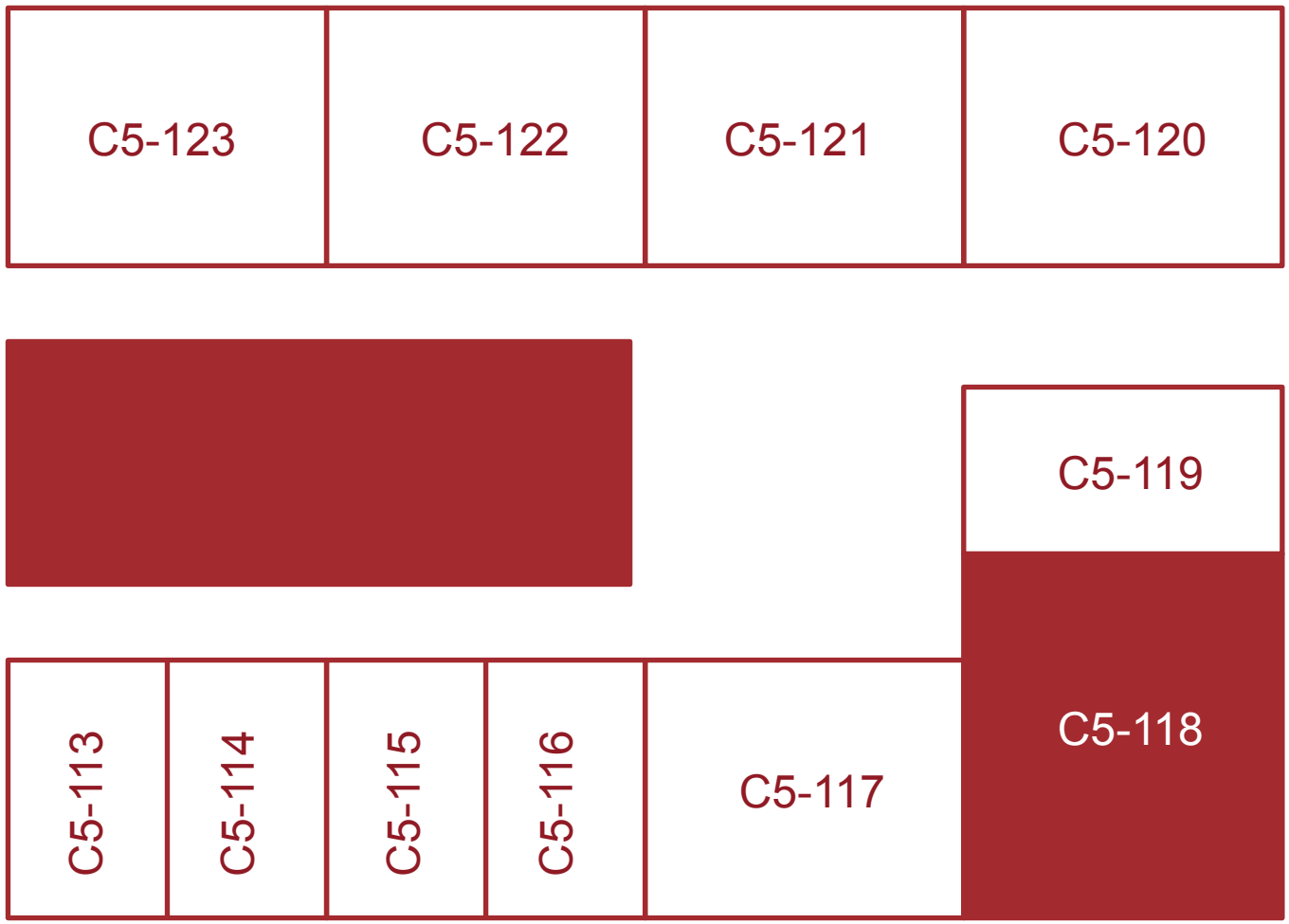

Sisyphus-I Protocol

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1) Thomas in C5-117	a) The head needs a central office, so that he is close to all members of the group. This should be a large office. b) This assignment is defined first, as the location of the office of the head restricts the possibilities of the subsequent assignments.	
2) Monika and Ulrika in C5-119	a) The secretaries' office should be located close to the office of the head. Both secretaries should work together in one large office. b) This assignment is executed as soon as possible, as its possible choices are extremely constrained.	
3) Eva in C5-116	a) The manager must have maximum access to the head and the secretariat. At the same time she should have a centrally located office. A small office will do. b) This is the earliest point where this decision can be taken.	
4) Joachim in C5-115	a) The heads of large projects should be close to the head and the secretariat.	b) There is no reason for the sequence of assignments of Joachim, Hans and Katharina.
5) Hans in C5-114		
6) Katharina in C5-113		
...		

Sisyphus-I YQT Members Data

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- From the protocol can be drawn data such as:

Name	Role	Project	Smoker	Hacker	Works with
Werner	Researcher	RESPECT	No	Yes	Angi, Marc
Mark	Researcher	KRITON	No	Yes	Angi, Werner
Andy	Researcher	TUTOR	Yes	No	
Harry	Researcher	BABYLON	No	Yes	Jurgen, Thomas
Thomas	Researcher	EULISP	No	No	Jurgen, Harry
Ulrike	Secretary		No	No	Thomas, Monika, Eva
Eva	Manager		No	No	Thomas, Ulrike, Monika
Kathatina	Researcher	MLT	Yes	Yes	
Jurgen	Researcher	EULISP	No	Yes	Thomas, Harry
...					

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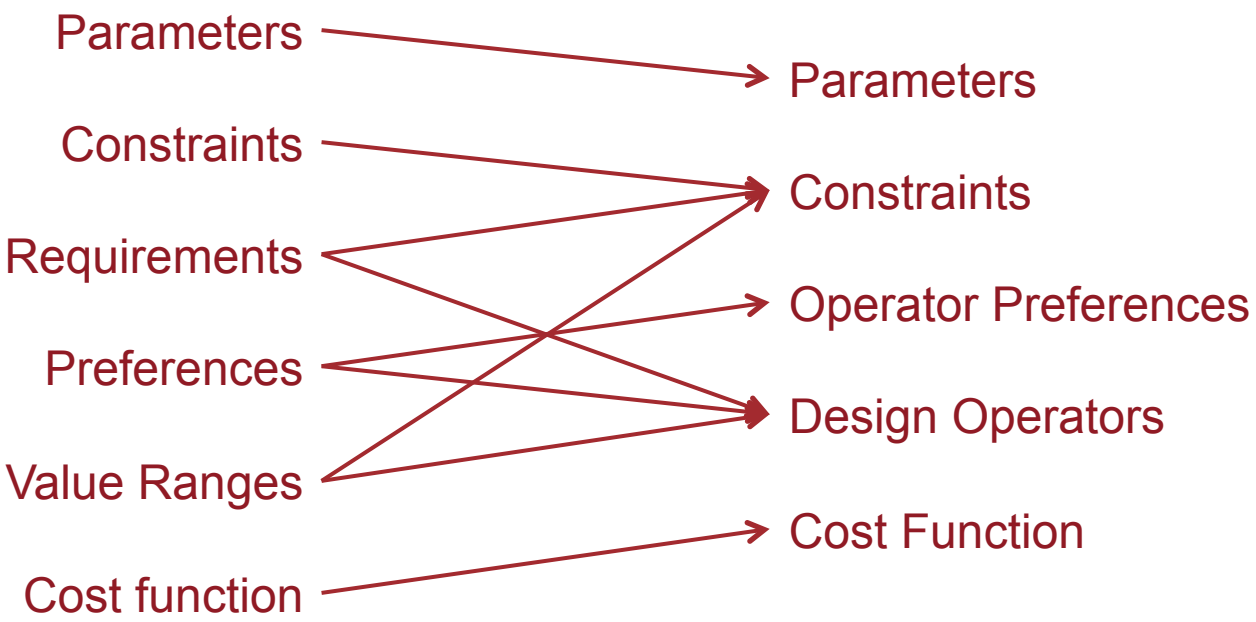
- The approach used rests on mapping from task concepts to method concepts as shown [Motta, 1999] :



Sisyphus-I Values Ranges

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- From the protocol can be drawn value ranges, based on given justifications in the protocol:

Type of YQT Member	Value Range	Justification
Head of group	All large, central offices	"The head needs a central office... This should be a large office"
Secretary	All large offices	"Secretaries should work together in one large office"
Manager	A centrally-located office	"should have a centrally located office"
Head-of-project	A single office	Siggi allocates them in single offices
Researcher	Any office	Siggi does not indicate any kind of constraints

- From the protocol can be drawn the following requirements and constraints:

Requirements	Constraints
R1. Head of group in large central office	C1. Do not exceed room size
R2. The secretaries' office has to be close to the office of the head	C2. Smokers cannot share with non-smokers
R3. Manager, head of group, and heads of projects do not share	
R4. Secretaries share the same room	
R5. Manager goes into central office	

Sisyphus-I Preferences

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- From the protocol can be drawn the following preferences:

Preference	Comment
P1. Head as close as possible to secretaries	The requirement specifies that they should be close. However, it makes sense to also add a preference so that solutions where the distance between the head and secretariat is minimised are given a higher ranking.
P2. Manager as close as possible to head and secretaries	Siggi talks about having maximum access to the head and the secretariat. This is modelled as a preference, stating that models which minimise the distance between the manager, the head and the secretaries are "better".
P3. Heads of large projects as close as possible to head and secretaries	Siggi actually talks about "heads of projects being close". However his solution does not satisfy his own requirement. Therefore this is modelled as a preference rather than a requirement.
P4. Members of same project should not share	Siggi states that members of the same project should not share. Again his solution does not satisfy this, so it is modelled as a preference.

Sisyphus-I Cost Function

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- Cost function produces a 4-dimensional vector,

  $<n_1, n_2, n_3, n_4>$, where:
  - n_1 measures the distance between the room of the head of group and that of the secretaries;
  - n_2 measures the distance between the manager's room and the rooms of the head of group and the secretaries;
  - n_3 measures the distance between the heads of projects and the head of group and secretaries;
  - n_4 provides a measure of the 'project synergy' afforded by a solution.

Sisyphus-I Cost Function (cntd.)

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- A design model in the Sisyphus-I domain d1, with cost function $<n_{11}, n_{12}, n_{13}, n_{14}>$ is cheaper than a design model d2, with cost $<n_{21}, n_{22}, n_{23}, n_{24}>$, iff one or more of the following conditions are satisfied:
  - $n_{11} < n_{21}$
  - $n_{11} = n_{21}$ and $n_{12} < n_{22}$
  - $n_{11} = n_{21}$ and $n_{12} = n_{22}$ and $n_{13} < n_{23}$
  - $n_{11} = n_{21}$ and $n_{12} = n_{22}$ and $n_{13} = n_{23}$ and $n_{14} < n_{24}$

- Solving by Gen-design-psm (Generic Model for Parametric Design), which enhances simple depth-first search via:
  - Focus selection – a DSR strategy analyses
    - **Value ranges** associated with each parameter,
    - The most constrained parameter in the **current design model**;
  - Operator selection – operator chosen according to given ordering.
- Solving by HC-design (Hill climbing) – same competence as Gen-design-psm, but much less efficient (measured at 10%, as compared to 78%).
- Solving by A*-design, based on heuristic function using estimated cost function – better competence (optimal solution), but comparable efficiency to HC-design.

EXTENSIONS

Application to Web Service Models

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- A standard language was developed for the description of PSMs called the Unified Problem-Solving Method Language (UPML) [Fensel et al, 2002]
- UPML was applied to the modelling of Web Services in the Web Service Modelling Framework (WSMF) [Fensel & Bussler, 2002]
- The WSMF approach was encoded in the Web Service Modeling Ontology (WSMO) – wherein ontology-based models are builts for goals (~tasks), services (~methods) and these are linked by mediators (~adapters) [Fensel et al., 2007]
- WSMO was encoded in a family of ontology languages, WSML, and an open-source implementation was carried out in WSMX.

SUMMARY

Summary

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- Problem-solving methods offer a means to structure and reuse elements of knowledge-based systems by abstracting from their domain.
- Efficiency is achieved by introducing assumptions that either restrict the size of the problem or that postulate strong requirements on the available domain knowledge.
- Adapters link tasks and PSMs to domains, allowing reuse of both, and express refinements between PSMs, allowing libraries to be built of these.

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Next Lecture

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Questions?

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